

Math 135 – Test 1

January 25, 2019

Name: Solution Set

Instructor: Patricia Wrean

No calculators are allowed for this test.

Total: 30 points

Part I: For these short-answer questions, you do not need to show any work. Place your final answer in the space provided. Each answer is worth one point.

1. (1 point) Simplify $\frac{20}{35}$.

4/7

$$\frac{20}{35} = \frac{\cancel{5} \times 4}{\cancel{5} \times 7} = \frac{4}{7}$$

2. (1 point) Write $3\frac{5}{8}$ as an improper fraction.

29/8

$$3\frac{5}{8} = \frac{24}{8} + \frac{5}{8} = \frac{29}{8}$$

3. (2 points) Multiply or divide, as indicated. Simplify when possible.

(a) $\frac{9}{8} \times \frac{4}{3} = \frac{3 \times \cancel{3} \times \cancel{4}}{2 \times \cancel{4} \times \cancel{3}} = \frac{3}{2}$

3/2

(or 1½)

(b) $\frac{7}{9} \div \frac{2}{9} = \frac{7}{\cancel{9}} \times \frac{\cancel{9}}{2} = \frac{7}{2}$

7/2

(or 3½)

4. (1 point) Write $\frac{17}{20}$ as a decimal.

0.85

$$\frac{17}{20} = \frac{17}{20} \left(\frac{5}{5} \right) = \frac{85}{100} = 0.85$$

or

$$\begin{array}{r} 20 \overline{) 17.0} \\ \underline{160} \\ 100 \\ \underline{100} \\ 0 \end{array}$$

Part II: For these questions, show your work and write your final answer in the space provided.

5. (2 points) Simplify the following fraction. Write your answer as a mixed number.

$$\frac{64}{56}$$

$$\underline{1\frac{1}{7}}$$

short version:

$$\frac{64}{56} = \frac{\cancel{8} \times 8}{\cancel{8} \times 7} = \frac{8}{7} = 1\frac{1}{7}$$

longer version:

$$\frac{64}{56} = \frac{\cancel{2} \times 32}{\cancel{2} \times 28} = \frac{\cancel{2} \times 16}{\cancel{2} \times 14} = \frac{\cancel{2} \times 8}{\cancel{2} \times 7} = \frac{8}{7} = 1\frac{1}{7}$$

6. (6 points) Add or subtract as indicated. Simplify when possible.

(a) $\frac{2}{3} + 2\frac{3}{4}$

$$\underline{3\frac{11}{12}}$$

$$\frac{2}{3} + 2\frac{3}{4} = \frac{2}{3} + \frac{11}{4} = \frac{2}{3} \left(\frac{4}{4}\right) + \frac{11}{4} \left(\frac{3}{3}\right) = \frac{8}{12} + \frac{33}{12} = \frac{41}{12}$$

$$\text{LCD} = 12$$

$$\text{or } 3\frac{5}{12}$$

(b) $\frac{5}{12} + \frac{17}{18} - \frac{1}{4} = \frac{5}{12} \left(\frac{3}{3}\right) + \frac{17}{18} \left(\frac{2}{2}\right) - \frac{1}{4} \left(\frac{9}{9}\right)$

$$\underline{2\frac{10}{9}}$$

$$= \frac{15}{36} + \frac{34}{36} - \frac{9}{36}$$

$$= \frac{40}{36}$$

$$= \frac{10 \times 4}{9 \times 4}$$

$$= \frac{10}{9}$$

$$\text{(or } 2\frac{10}{9}\text{)}$$

LCD:

$$12 = 2 \times 2 \times 3$$

$$18 = 2 \times 3 \times 3$$

$$4 = 2 \times 2$$

$$\text{so LCD} = 2 \times 2 \times 3 \times 3 = 36$$

7. (5 points) Multiply or divide as indicated. Simplify when possible.

$$(a) \frac{15}{24} \times \frac{8}{9} = \frac{\cancel{5} \times \cancel{8}}{\cancel{8} \times \cancel{3}} \times \frac{\cancel{8}}{9} = \frac{5}{9}$$

5/9

$$(b) \frac{\frac{5}{6}}{2\frac{1}{2}} = \frac{5/6}{5/2}$$

$$= \frac{5}{6} \times \frac{2}{5}$$

$$= \frac{\cancel{5}}{\cancel{2} \times 3} \times \frac{\cancel{2}}{\cancel{5}} = \frac{1}{3}$$

1/3

8. (5 points) Add, subtract, multiply, or divide as indicated. Leave your answer in decimal form. Do not round your answer.

$$(a) 128.53 - 92.9$$

35.63

$$\begin{array}{r} 128.53 \\ - 92.9 \\ \hline 35.63 \end{array}$$

$$(b) 1.681 \div 2.05 = \frac{1.681}{2.05} \left(\frac{100}{100} \right) = \frac{168.1}{205}$$

0.82

$$\begin{array}{r} 205 \overline{) 168.1} \\ \underline{1640} \\ 410 \\ \underline{410} \\ 0 \end{array}$$

9. (2 points) What percent of 40 is 24?

60%

$$\frac{24}{40} = \frac{6 \times 4}{10 \times 4} = \frac{6}{10} = 0.6 = 60\%$$

10. (2 points) While playing hockey, Kirsten attempted 120 shots on goal this season. If 15% of her shots were successful, how many goals did she score? Write a concluding sentence for your answer.

$$\begin{aligned} \text{goals scored} &= 15\% \text{ of } 120 \\ &= 0.15 \times 120 \\ &= 18 \end{aligned}$$

$$\begin{array}{r} 120 \\ 0.15 \\ \hline 600 \\ 120 \\ \hline 18.00 \end{array}$$

Kirsten scored 18 goals.

11. (3 points) Sanjay wants to replace his old deck. The deck is 8.5 ft by 14 ft. If the new decking costs \$6.20 per square foot, how much will it cost Sanjay to replace the deck? Write a concluding sentence for your answer.

$$\begin{aligned} \text{area of deck} &= \text{length} \times \text{width} \\ &= 8.5 \times 14 \\ &= 119 \text{ ft}^2 \end{aligned}$$

$$\begin{array}{r} 8.5 \\ 14 \\ \hline 340 \\ 85 \\ \hline 119.0 \end{array}$$

$$\begin{aligned} \text{total cost} &= \text{cost/ft}^2 \times \text{area} \\ &= 6.20 \times 119 \\ &= \$737.80 \end{aligned}$$

$$\begin{array}{r} 119 \\ 6.2 \\ \hline 238 \\ 714 \\ \hline 737.8 \end{array}$$

Sanjay's new deck will cost \$737.80