

Section 4.1: Big O and Rates of Growth

Tuesday, February 11, 2020 12:07 PM

Growth

example: suppose you wish to get digital copies of a number of Star Trek episodes. You can either download them at one episode per hour, or you can get overnight delivery from Amazon (call it 24 hour delivery).

scenarios: we want minimum delivery time (1h/episode vs. 24 hours)

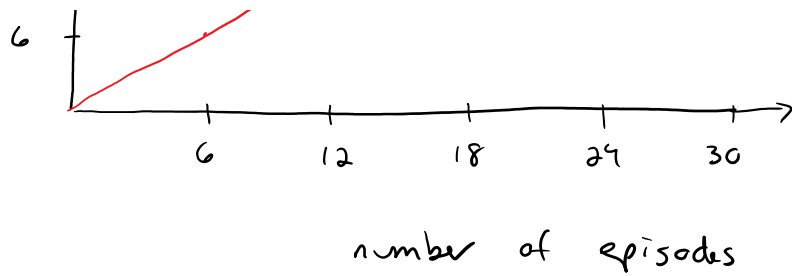
few episodes (< 24), downloading is faster

break even ($= 24$), both methods take same time

many episodes (> 24), overnight is faster

and if you don't know how many episodes, then the "many episodes" scenario is the safest approach





conditions

2020/02/12

number of steps required for algorithms:

consider adding two 5-digit numbers:

$$\begin{array}{r} 12345 \\ + 12345 \\ \hline \end{array}$$

best case: 5 additions
 worst case: 5 additions plus some "carries"

consider multiplying two 5-digit numbers:

$$\begin{array}{r} 12345 \\ \times 12345 \\ \hline \text{xxxxx} \\ \text{xxxxx} \\ \text{xxxxx} \\ \text{xxxxx} \\ \text{xxxxx} \\ \hline \end{array}$$

best case:
 25 multiplications plus 9 column additions and no carries

worst case: many more

the worrying part is the fact that the number of multiplications goes as the square of the

the worrying part is the fact that the number of multiplications goes as the square of the number of digits

100 digits \rightarrow 10000 multiplications! ouch!

addition: if you double the number of digits, you approximately double the number of operations

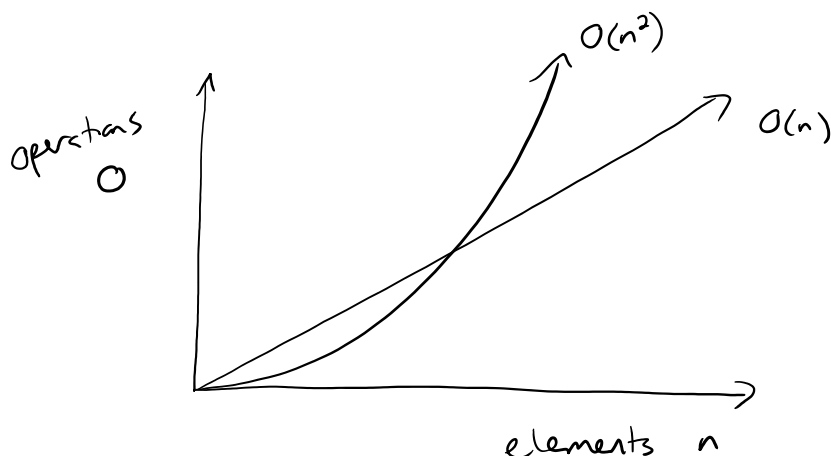
Big O notation: $O(n)$

"order n"

multiplication: if you double the number of digits, you approximately quadruple the number of operations

$O(n^2)$

note: I will not ask you to analyse an algorithm to figure out Big O.



2020/02/13

Big O deals with the number of operations
required for large n

(for small n , lines could intersect)

→ for the graph above, for sufficiently large n ,
 $O(n^2)$ is greater than $O(n)$