

Review:

Thursday, March 17, 2016
11:03 AM

factor into linear factors:

$$f(x) = x^3 - 8x - 3$$

$$\frac{p}{q} = \frac{\pm 1, \pm 3}{\pm 1} = \pm 1, \pm 3$$

$$f(1) \neq 0$$

$$f(-1) \neq 0$$

$$f(3) = 0 \quad \checkmark$$

so $(x-3)$ is a factor

$$\begin{array}{r} x^2 + 3x + 1 \\ x-3 \overline{) x^3 + 0x^2 - 8x - 3} \\ \underline{x^3 - 3x^2} \\ 3x^2 - 8x \\ \underline{3x^2 - 9x} \\ x - 3 \end{array}$$

$$x^2 + 3x + 1 = 0$$

$$\begin{aligned} x &= \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \\ &= \frac{-3 \pm \sqrt{9 - 4}}{2} \\ &= \frac{-3 \pm \sqrt{5}}{2} \end{aligned}$$

$$\begin{aligned} f(x) &= (x-3) \left(x - \frac{-3+\sqrt{5}}{2} \right) \left(x - \frac{-3-\sqrt{5}}{2} \right) \\ &= (x-3) \left(x + \frac{3-\sqrt{5}}{2} \right) \left(x + \frac{3+\sqrt{5}}{2} \right) \end{aligned} \quad \left. \vphantom{f(x)} \right\} \text{Linear factors}$$

Solve:

$$\ln x + \ln(1-x) = \ln(2x-12)$$

$$\ln x(1-x) = \ln(2x-12)$$

$$x(1-x) = 2x-12$$

$$x-x^2 = 2x-12$$

$$0 = x^2 + x - 12$$

$$0 = (x-3)(x+4)$$

$$x = \cancel{3}, \cancel{-4}$$

\emptyset