

Section V.4: Cross Product

Exercises

1. Vector \mathbf{A} is in the y -direction, while vector \mathbf{B} is in the negative x -direction. What is the direction of $\mathbf{A} \times \mathbf{B}$? $\mathbf{B} \times \mathbf{A}$?
2. Vector \mathbf{A} is in the z -direction, while vector \mathbf{B} is in the y -direction. What is the direction of $\mathbf{A} \times \mathbf{B}$? $\mathbf{B} \times \mathbf{A}$?

Calculate the cross product $\mathbf{A} \times \mathbf{B}$ for the following vectors.

3. $\mathbf{A} = \mathbf{i}$, $\mathbf{B} = \mathbf{j}$
4. $\mathbf{A} = \mathbf{j}$, $\mathbf{B} = \mathbf{i}$
5. $\mathbf{A} = \mathbf{i}$, $\mathbf{B} = \mathbf{k}$
6. $\mathbf{A} = \mathbf{k}$, $\mathbf{B} = \mathbf{i}$
7. $\mathbf{A} = \mathbf{k}$, $\mathbf{B} = \mathbf{j}$
8. $\mathbf{A} = \mathbf{j}$, $\mathbf{B} = \mathbf{j}$
9. $\mathbf{A} = 2\mathbf{i} - 9\mathbf{j} - \mathbf{k}$, $\mathbf{B} = 3\mathbf{i} + \mathbf{j} - 4\mathbf{k}$
10. $\mathbf{A} = 12\mathbf{i} - 5\mathbf{k}$, $\mathbf{B} = 3\mathbf{i} + \mathbf{j} - 4\mathbf{k}$
11. $\mathbf{A} = \mathbf{k}$, $\mathbf{B} = 3\mathbf{i} + 2\mathbf{j} - 7\mathbf{k}$
12. $\mathbf{A} = 2\mathbf{i} - \mathbf{j}$, $\mathbf{B} = 2\mathbf{i} - \mathbf{k}$
13. $\mathbf{A} = 5\mathbf{i} + 6\mathbf{j} - 7\mathbf{k}$, $\mathbf{B} = \mathbf{i} + 12\mathbf{j} - 2\mathbf{k}$
14. Consider your answer to #13. What's the magnitude of the vector in your answer?
15. [tricksy] Consider the following pair of vectors: $\mathbf{A} = -9\mathbf{j} - 4\mathbf{k}$, $\mathbf{B} = 3\mathbf{i} + 5\mathbf{j}$

Calculate the angle between these vectors using

- a) the dot product
- b) the cross product

Are your answers for a) and b) the same? If not, what happened? And why is the dot product the preferred method here?