

Section 3.1: cont'd

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10:31 AM

recall: $\mu = E(x) = \sum x p(x)$

variance:

$$\begin{aligned}\sigma^2 &= E(x - \mu)^2 \\ &= \sum (x - \mu)^2 p(x) \quad \leftarrow \text{formal definition} \\ &\quad \text{(annoying to calculate)} \\ &= \sum x^2 p(x) - \mu^2 \quad \leftarrow \text{calculation formula} \\ &\quad \text{(less annoying to calculate)}\end{aligned}$$

standard deviation: $\sigma = \sqrt{\sigma^2}$

example: consider the probability distribution given below. calculate the mean and standard deviation of x .

x	$p(x)$
0	$\frac{4}{10}$
1	$\frac{6}{10}$
2	$\frac{3}{10}$

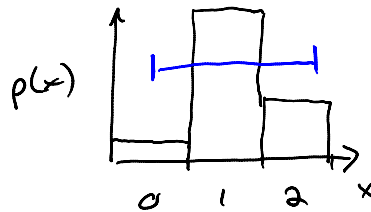
$$\begin{aligned}\mu = E(x) &= \sum x p(x) \\ &= 0 \cdot \frac{4}{10} + 1 \cdot \frac{6}{10} + 2 \cdot \frac{3}{10} \\ &= 1.2\end{aligned}$$

$$\begin{aligned}\sigma^2 &= \sum x^2 p(x) - \mu^2 \\ &= 0^2 \cdot \frac{4}{10} + 1^2 \cdot \frac{6}{10} + 2^2 \cdot \frac{3}{10} - (1.2)^2\end{aligned}$$

$$= 0.36$$

$$\sigma = 0.6$$

note: $\mu \pm 2\sigma = 1.2 \pm 2(0.6)$
 $=$ from 0 to 2.4



example: what is the expected value for winning the jackpot on BC Lotto 6/49 when the pot is 2.2 million dollars? Assume that there is only one winning ticket and it cost \$2 to play.

how many tickets in total? ${}_{49}C_6 = 13\,983\,816$

odds of winning jackpot? $\frac{1}{13\,983\,816}$

x : either you lose \$2

or you win \$2.2 million (though you still have paid \$2)

x	$p(x)$
-2	$1 - \frac{1}{13\,983\,816}$
$2.2 \times 10^6 - 2$	$\frac{1}{13\,983\,816}$

$$\begin{aligned}
E(x) &= \sum x p(x) \\
&= -2 \left(1 - \frac{1}{13983816} \right) + (2.2 \times 10^6 - 2) \frac{1}{13983816} \\
&= -2 + \frac{2.2 \times 10^6}{13983816} \\
&= -1.84
\end{aligned}$$

On average, you lose \$1.84 each time you play.

discrete random variables are used for a variety of everyday situations

→ there are some very common scenarios that have named distributions associated with them

we will look at two of them:

- binomial
- poisson