

Section 8: cont'd

Monday, April 10, 2017 1:01 PM

(10) breaking strength of rope \rightarrow normally distributed

8 ropes

$$\bar{x} = 62.1 \text{ lbs}$$

$$SD = 2.5 \text{ lbs}$$

want 90% LCB for mean breaking strength of this brand of rope

small sample size \rightarrow t dist

$$\mu = \bar{x} - t_{\alpha} \frac{s}{\sqrt{n}}$$

α because it's a one-sided confidence interval

want 90% LCB

$\underbrace{\quad}_{1-\alpha}$

so $\alpha = 0.1$ with $df = n-1 = 7$

$$t_{\alpha} = t_{0.1} = 1.415$$

$$\begin{aligned} \mu &= \bar{x} - t_{\alpha} \frac{s}{\sqrt{n}} \\ &= 62.1 - 1.415 \left(\frac{2.5}{\sqrt{8}} \right) \end{aligned}$$

$$= 60.8 \text{ lbs}$$

Summary: confidence intervals

| | Confidence interval | LCB or UCB |
|-----------------------------|---------------------------|--------------|
| large sample $n \geq 30$ | $Z_{\alpha/2}$ normal | Z_{α} |
| small sample $n < 30$ | $t_{\alpha/2}$ t-table | t_{α} |