

Section 1.1: The Geometry and

Tuesday, September 7, 2021 11:57 AM

Algebra of vectors

vectors in the plane:

a vector is a directed line segment that corresponds to a displacement from one point A to another point B

in general, A and B have coordinates (x_1, y_1) and (x_2, y_2) for 2D vectors

↑ points have round brackets

then vector \vec{AB} can be written as

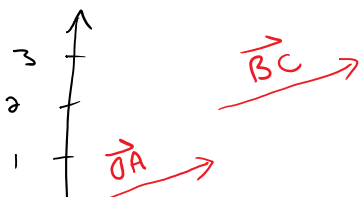
$$[x_2 - x_1, y_2 - y_1]$$

written as a row vector $[3, -2]$

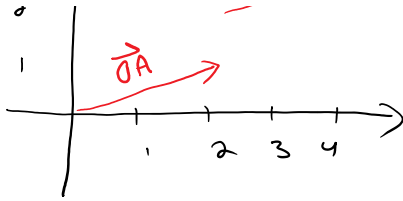
can also write as column vector $\begin{bmatrix} 3 \\ -2 \end{bmatrix}$

2021/09/08

equality of vectors



these two vectors are equal



equal

vector \vec{OA} is said to be in standard position since tail is at the origin

one convention:

$$\vec{OA} = \vec{A}$$

↑
O for origin

notation: in 2D:

$$\vec{0} = [0, 0]$$

the zero vector

← hard to draw!
but a perfectly good vector

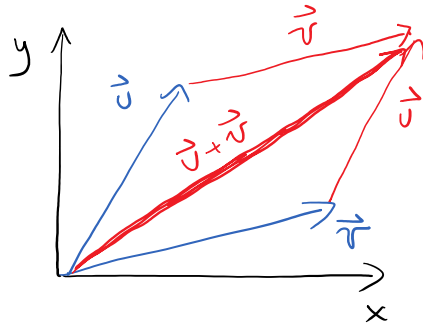
the set of all vectors with two components is written

$$\mathbb{R}^2 \quad (\text{pronounced "R two"})$$

$$\mathbb{R}^3 \quad - \text{three components}$$

$$\mathbb{R}^n \quad - n \text{ components}$$

vector addition:



$$\vec{u} + \vec{v} = [u_1 + v_1, u_2 + v_2]$$

note: order doesn't matter

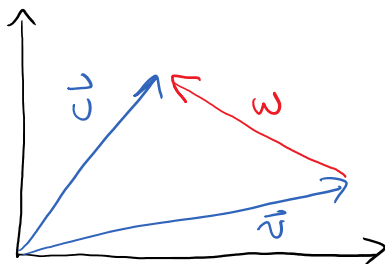
scaling a vector:

\vec{v} is a vector

c is a constant

$$\text{if } \vec{v} = [v_1, v_2], \text{ then } c\vec{v} = [cv_1, cv_2]$$

vector subtraction:



$$\vec{u} + \vec{w} = \vec{u}$$

$$\vec{w} = \vec{u} - \vec{v}$$

linear combination of vectors: definition is on handout

example: $\vec{w} = -3 \begin{bmatrix} 1 \\ 1 \end{bmatrix} + 2 \begin{bmatrix} 0 \\ 2 \end{bmatrix}$

↑ ↑
coefficients

then \vec{w} is a linear combination of $\begin{bmatrix} 1 \\ 1 \end{bmatrix}$ and $\begin{bmatrix} 0 \\ 2 \end{bmatrix}$