

## Section 1.6: Measures of Centre

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numerical measures - another way to summarize a data set

(graphs  $\rightarrow$  visual summary)

- particularly of use when comparing two data sets whose values are very similar

numerical measures

$\rightarrow$  called parameters for populations  
 $\rightarrow$  called statistics for samples

we'll look at:

measures of centre

measures of dispersion (spread/variability)

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measures of centre:

mean (average): add all data points, divide by the number of data points

population mean:

$$\mu = \frac{\sum_{i=1}^n x_i}{n}$$

Greek letter  
"mu"

where  $x_i$  is the  $i^{\text{th}}$

measurement  
 $n$  is the size of  
the population

sample mean:

$$\bar{x} \quad \text{"x-bar"} = \frac{\sum x_i}{n}$$

one problem: greatly affected by "outliers"

↑

data points far  
from the majority  
of points

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median - if you write your data as an ordered list, it's the middle value

- if you have an even number of data points, it's the average of the two middle points

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example: starting salary for Bridge graduates

\$ 60 000  
\$ 50 000  
\$ 58 000  
\$ 59 500  
\$ 1 500 000

\$ 1 500 000

find the mean and median for this sample.

$$\begin{aligned} \text{mean} &= \bar{x} = \$ 345\,500 \\ \text{median} &= \$ 59\,500 \end{aligned}$$

by the way, there is no universally recognized symbol for the median. Some use  $\tilde{x}$  (x-tilde)

note: if there are lots of data points, how do you determine which is the middle one?

$$\text{position} = \frac{1}{2}(n+1)$$

for 75 points, the median is the 38<sup>th</sup> point  
76

38.5<sup>th</sup>

take average  
of 38<sup>th</sup> and 39<sup>th</sup> points

mode - most common value in a data set  
(rarely used in science/engineering because most data is continuous)

one last thing about the mean:  
suppose you have summarized a data set in a

one last thing about the mean.

suppose you have summarized a data set in a table:

x	f
1	5
2	2
3	4

called a "frequency" table

↑ values of x  
↑ number of times they occur

$$\bar{x} = \frac{\sum x_i \cdot f_i}{n} = \frac{1 \cdot 5 + 2 \cdot 2 + 3 \cdot 4}{11} = \sum f_i$$